

Qn 1

$$a) f(x) = (x-3)^2(x^2+6)^5$$

Let $u = (x-3)$
and $v = (x^2+6)$

$$f(x) = u^2 v^5$$

$$\frac{dy}{dx} = 2u v^5 + 5u^2 v^4 \quad (\text{Chain rule})$$

$$\therefore = 2(x-3)(x^2+6)^5 + 5(x-3)^2(x^2+6)^4$$

$$= (x-3)(x^2+6)^4 (2(x^2+6) + 5(x-3))$$

b) ~~f(x)~~

$$f(x) = \frac{x^2 + 4x + 3}{x+3}$$

$$= \frac{(x+3)(x+1)}{(x+3)}$$

$$f(x) = x+1$$

$$f'(x) = 1 \cdot x^{-1}$$

$$= \underline{\underline{1}}$$

Qn 3

$$f(x) = \frac{8}{3+x}$$

Let $(3+x) = u$

$$f(u) = \frac{8}{u}$$

$$f'(u) = 8 \cdot \frac{1}{u^2}$$

$$= 8 \ln(3+x)$$

at point (1, 2)

$$\text{Gradient} = 8 \ln(4)$$

$$= 11.09$$

y Intercept

$$g = \frac{8}{3} =$$

~~function~~
Equation

$$y = 11.09x + 2.33$$

Qn 3

$$f(4) = 5, \quad f'(4) = 3$$

$$f'(7) = 9$$

$$g(4) = 12, \quad g'(4) = 6$$

$$\begin{array}{r} f'(4) + c = 3 \\ f'(7) + c = 9 \\ \hline \end{array} \Rightarrow \begin{array}{r} 4u + c = 3 \\ 7u + c = 9 \\ \hline -3u = -6 \\ u = 2 \\ c = -5 \end{array}$$

$$f'(x) = 2x - 5$$

$$f(x) = x^2 - 5x + c$$

$$f(4) \Rightarrow 5 = (4)^2 - 5(4) + c$$

$$c = 9$$

$$f(x) = x^2 - 5x + 9$$

$$(fg)'(4) = f'(4) \cdot g'(4)$$

$$= 3 \times 6$$

$$= \underline{\underline{18}}$$

Qn 4

$$\text{Tangent} = \frac{dy}{dx} = 6x$$

$$\frac{y}{x} = \frac{6x}{x}$$

$$x = 1$$

$$\text{at } x = 1 \quad y = 3(1)^2 = 3$$

$$\frac{dy}{dx} = \frac{y-3}{x-1}$$

$$y - 3 = 6x - 6$$

$$y = 6x - 3$$

$$b = \underline{\underline{-3}}$$

Qns 5

$$y = -x^3 + 3x^2 - 2$$

$$\frac{dy}{dx} = -3x^2 + 6x$$

Horizontal

$$-3x^2 + 6x = 0$$

$$x(-3x + 6) = 0$$

$$x = 0$$

$$\text{or } -3x = -6$$

$$x = 2$$

When $x = 0$

$$y = -2$$

or

When $x = 2$

$$y = -(2)^3 + 3(2)^2 - 2$$
$$= 2$$

$$x + 4 = 3$$
$$x + 7 = 9$$

f(x)

$$4x + c = 3$$

$$-7x + c = 9$$

$$3x = 6$$

$$x = 2$$

$$2x + 5 =$$

Qsn. 6

$$C(x) = -0.004x^2 + 5.2x + 2500$$

$$C'(x) = -0.008x + 5.2$$

$$R(x) = 218 - 0.36x$$

$$\text{Profit } P(x) = 218x - 0.18x^2 + 0.004x^2 - 5.2x - 2500$$
$$= 212.8x - 0.176x^2 - 2500$$

Marginal Profit = $P'(x)$

$$P'(x) = 212.8 - 0.352x$$

$$P'(150) = 212.8 - 0.352(150)$$

$$= \underline{\underline{160}}$$